

- 1.1.25.** If $f(x) = 3x^2 - x + 2$, find $f(2)$, $f(-2)$, $f(a)$, $f(-a)$, $f(a + 1)$, $2f(a)$, $f(2a)$, $f(a^2)$, $[f(a)]^2$, and $f(a + h)$.
- 1.1.27.** Evaluate the difference quotient $\frac{f(3+h)-f(3)}{h}$ for the function $f(x) = 4 + 3x - x^2$. Simplify your answer.
- 1.1.29.** Evaluate the difference quotient $\frac{f(x)-f(a)}{x-a}$ for the function $f(x) = \frac{1}{x}$. Simplify your answer.
- 1.1.31.** Find the domain of $f(x) = \frac{x+4}{x^2-9}$.
- 1.1.33.** Find the domain of $f(t) = \sqrt[3]{2t-1}$.
- 1.1.35.** Find the domain of $h(x) = \frac{1}{\sqrt[4]{x^2-5x}}$.
- 1.1.37.** Find the domain of $F(p) = \sqrt{2 - \sqrt{p}}$.
- 1.1.47.** Find the domain and sketch the graph of $f(x) = \begin{cases} x + 2 & \text{if } x < 0 \\ 1 - x & \text{if } x \geq 0 \end{cases}$.
- 1.1.49.** Find the domain and sketch the graph of $f(x) = \begin{cases} x + 2 & \text{if } x \leq -1 \\ x^2 & \text{if } x > -1 \end{cases}$.
- 1.1.51.** Find an expression for the function whose graph is the line segment joining the points $(1, -3)$ and $(5, 7)$.
- 1.1.57.** A rectangle has perimeter 20. Express the area of the rectangle as a function of the length of one of its sides.
- 1.1.61.** An open rectangular box with volume of 2 cubic meters has a square base. Express the surface area of the box as a function of the length of a side of the base.
- 1.1.65.** In a certain state the maximum speed permitted on freeways is 65 mph and the minimum speed is 40 mph. The fine for violating these limits is \$15 for every mile per hour above or below the limits. Express the amount of the fine as a function $F(x)$ of the driving speed.
- 1.2.5.** Find an equation for the family of linear functions with slope 2, and sketch several members of the family. Find an equation for the family of linear functions such that $f(2) = 1$ and sketch several members of the family. Which function belongs to both families?
- 1.2.7.** What do all members of the family of linear functions $f(x) = c - x$ have in common? Sketch several members of the family.
- 1.2.9.** Find an expression for a cubic function f such that $f(1) = 6$ and $f(-1) = f(0) = f(2) = 0$.
- 1.2.13.** The relationship between the Fahrenheit and Celsius temperature scales is given by the linear function $F = \frac{9}{5}C + 32$. What is the slope of this function, and what does it represent? What is the F -intercept of this function and what does it represent?
- 1.2.17.** At the surface of the ocean, the water pressure is 15 pounds per square inch; below the surface, the water pressure increases by 4.34 pounds per square inch for every 10 feet of descent. Express the water pressure as a function of depth, and determine at which depth the pressure reaches 100 pounds per square inch.
- 1.3.1.** For a given function f , write equations for the functions whose graphs are the following transformations of f 's graph:

- shift three units upwards.
- shift three units downwards.
- shift three units to the right.
- shift three units to the left.
- reflect about the x -axis.
- reflect about the y -axis.
- stretch vertically by a factor of 3.

1.3.9. Graph the function $y = \frac{1}{x+2}$ by hand, not by plotting points, but by transforming a standard function's graph.

1.3.13. Graph the function $y = \sqrt{x-2} - 1$ by hand, not by plotting points, but by transforming a standard function's graph.

1.3.21. Graph the function $y = |x - 2|$ by hand, not by plotting points, but by transforming a standard function's graph.

1.3.23. Graph the function $y = |\sqrt{x} - 1|$ by hand, not by plotting points, but by transforming a standard function's graph.

1.3.31. For $f(x) = x^2 - 1$ and $g(x) = 2x + 1$, find $f \circ g$, $g \circ f$, $f \circ f$, and $g \circ g$, and identify their domains.

1.3.35. For $f(x) = x + \frac{1}{x}$ and $g(x) = \frac{x+1}{x+2}$, find $f \circ g$, $g \circ f$, $f \circ f$, and $g \circ g$, and identify their domains.

1.3.41. Express $F(x) = (2x + x^2)^4$ in the form $f \circ g$.

1.3.43. Express $F(x) = \frac{\sqrt[3]{x}}{1+\sqrt[3]{x}}$ in the form $f \circ g$.

1.3.45. Express $v(t) = \sec(t^2) \tan(t^2)$ in the form $f \circ g$.

1.R.TF1. Determine whether the statement "If f is a function, then $f(s+t) = f(s) + f(t)$ " is true or false. If true, explain why; if false, explain why or give a counterexample.

1.R.TF3. Determine whether the statement "If f is a function, then $f(3x) = 3f(x)$ " is true or false. If true, explain why; if false, explain why or give a counterexample.

1.R.TF5. Determine whether the statement "A vertical line intersects the graph of a function at most once" is true or false. If true, explain why; if false, explain why or give a counterexample.

1.R.E3. If $f(x) = x^2 - 2x + 3$, evaluate the difference quotient $\frac{f(a+h)-f(a)}{h}$.

1.R.E5. Find the domain and range of $f(x) = \frac{2}{3x-1}$.

1.R.E9. If $y = f(x)$ has a given graph, describe how the graphs of the following functions can be obtained from the graph of f :

- $y = f(x) + 8$.
- $y = f(x + 8)$.
- $y = 1 + 2f(x)$.
- $y = f(x - 2) - 2$.
- $y = -f(x)$.
- $y = f^{-1}(x)$.

1.R.E11. Use transformations to sketch the graph of $y = -\sin 2x$.

1.R.E13. Use transformations to sketch the graph of $y = \frac{1}{2}(1 + e^x)$.

1.R.E15. Use transformations to sketch the graph of $y = \frac{1}{x+2}$.