

Show all work for problems 3-5; use the back of the sheet if necessary.

1. **(4 points)** Answer the following form-conversion problems.

(a) **(2 points)** Express the interval $(-2, 5]$ in terms of inequalities.

The parenthesis indicates a non-inclusive inequality; the square bracket indicates an inclusive inequality, so this interval can be described as $-2 < x \leq 5$.

(b) **(2 points)** Express the inequality $x > -1$ in interval notation.

Since this interval does not include its lower bound, we would use a parenthesis for the left boundary. Since there is no bound on the right, we use the peculiar infinite-boundary notation to give interval $(-1, \infty)$ or $(-1, +\infty)$.

2. **(2 points)** Evaluate the expression $4^{-3/2}$.

Since this has a negative exponent, we might start by rewriting it as $\frac{1}{4^{3/2}}$. This can be decomposed as $\frac{1}{(4^{1/2})^3} = \frac{1}{\sqrt{4}^3}$, or as $\frac{1}{[(4)^3]^{1/2}} = \frac{1}{\sqrt{4^3}}$. Both will give you the same answer, but the former is much easier to evaluate:

$$\frac{1}{\sqrt{4}^3} = \frac{1}{2^3} = \frac{1}{8}$$

$$\frac{1}{\sqrt{4^3}} = \frac{1}{\sqrt{64}} = \frac{1}{8}$$

3. **(3 points)** Simplify the rational expression $\frac{x}{x+2} - \frac{3}{2x-1}$.

$$\frac{x}{x+2} - \frac{3}{2x-1} = \frac{x(2x-1)}{(x+2)(2x-1)} - \frac{3(x+2)}{(x+2)(2x-1)} = \frac{x(2x-1) - 3(x+2)}{(x+2)(2x-1)} = \frac{2x^2 - 4x - 6}{2x^2 + 3x - 2}$$

4. **(3 points)** Expand the polynomial $2x^3 - (x^2 - x)(x + 2)$.

$$\begin{aligned} 2x^3 - (x^2 - x)(x + 2) &= 2x^3 - (x^3 + 2x^2 - x^2 - 2x) \\ &= 2x^3 - x^3 - 2x^2 + x^2 + 2x \\ &= x^3 - x^2 + 2x \end{aligned}$$

5. **(3 points)** Using any method you like, solve the equation $x^2 - 3x = 6$.

We start by writing the entire quadratic on a single side of the equation, as $x^2 - 3x - 6 = 0$. Then, using the quadratic formula:

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \cdot 1(-6)}}{2} = \frac{3 \pm \sqrt{33}}{2}$$