

1. **(6 points)** *Bill distributed \$1000 between two investments: a CD which returns 1% annual interest, and a mutual fund which returns 3% annual interest. He earned a total of \$18 in interest after a year. How much money did he put into each investment?*

Let us denote the quantity put into the CD as  $x$ ; since the remainder went into the mutual fund, we can denote the quantity in the mutual fund as  $1000 - x$ . Then, the interest on the  $x$  dollars earning 1% interest is  $0.01x$  dollars, while the interest on the  $1000 - x$  dollars earning 3% interest is  $0.03(1000 - x)$  dollars. Since the total interest is \$18, we know that:

$$\begin{aligned} 0.01x + 0.03(1000 - x) &= 18 \\ 0.01x + 30 - 0.03x &= 18 \\ -0.02x &= -12 \\ x &= 600 \end{aligned}$$

so \$600 are in the CD, and \$400 are in the mutual fund.

2. **(3 points)** *Solve the linear inequality  $2x + 2 < 7x - 1$ ; you may express the solution either in terms of  $x$  or in interval notation.*

$$\begin{aligned} 2x + 2 &< 7x - 1 \\ -5x + 2 &< -1 \\ -5x &< -3 \\ x &> \frac{3}{5} \end{aligned}$$

so one could answer with either the inequality  $x > \frac{3}{5}$  or the interval  $(\frac{3}{5}, \infty)$ .

3. **(4 points)** *Find an equation of the line through  $(-2, 5)$  and  $(1, -1)$ .*

First we calculate the line's slope, based on the two points:

$$m = \frac{-1 - 5}{1 - (-2)} = \frac{-6}{3} = -2$$

and then, based on the slope, we could use point-slope form with either of the two points (here we use  $(1, -1)$  as an example):

$$y - (-1) = -2(x - 1)$$

which could be written in slope-intercept form, if desired:

$$y = -2x + 1$$

4. **(3 points)** *Given the piecewise function  $f(x) = \begin{cases} 5 & \text{if } x \leq 2 \\ 2x - 3 & \text{if } x > 2 \end{cases}$ , calculate the values of the following expressions:*

- $f(1)$ .

Since  $1 \leq 2$ ,  $f(1) = 5$ .

- $f(2)$ .

Since  $2 \leq 2$ ,  $f(2) = 5$ .

- $f(3)$ .

Since  $3 > 2$ ,  $f(3) = 2 \cdot 3 - 3 = 3$ .

5. (4 points) Find the domain of the function  $g(x) = \sqrt{7 - 3x}$ .

We identify the places where this function is in calculable: since it contains a square root, we must consider the prospect that the argument of the square root might be negative. Thus, the function cannot be calculated if  $7 - 3x < 0$ ; rearranging and solving this inequality gives  $x > \frac{7}{3}$ . Since this is the set of points where  $f(x)$  cannot be found, the domain is simply all the other points, i.e. when  $x \leq \frac{7}{3}$ , or, in interval notation,  $(-\infty, \frac{7}{3}]$ .