

3. **(23 points)** Evaluate the following limits; if they cannot be evaluated, show why not.

(a) $\lim_{x \rightarrow 0} \frac{xe^x}{e^x - 1 - x}$.

(b) $\lim_{x \rightarrow +\infty} \frac{\ln x}{\sqrt{x}}$.

(c) $\lim_{x \rightarrow 0} \frac{e^x - e^{-x}}{\sin x}$.

(d) $\lim_{\theta \rightarrow 0} \sin \theta \csc(5\theta)$.

(e) $\lim_{u \rightarrow 0} \frac{u^2 - \cos u}{\sqrt[3]{u} + \sin u}$.

4. **(17 points)** Answer the following questions:

(a) **(9 points)** Find $h(x)$ given that $h'(x) = \frac{3}{x^2} + \sqrt{x}$ and $h(9) = 16$.

(b) **(8 points)** Find the general antiderivative of $g(u) = u^3 - 5 + 6u^2 + \frac{8}{\sqrt{1-u^2}} - \frac{3}{\sqrt{u}}$.

5. **(24 points)** Answer the following questions related to the shape of the graph of the function $f(x) = e^x(x^2 - 6x + 10)$.

(a) **(6 points)** Where is $f(x)$ increasing? Where is it decreasing? Label which is which.

(b) **(6 points)** What are its critical points, and is each a local maximum, a local minimum, or neither?

(c) **(4 points)** What are $f(x)$'s long term behaviors as x grows very large and as x grows very negative? Describe each direction in either words or symbols.

(d) **(8 points)** Where is it concave up? Where is it concave down? Label which is which. Where, if anywhere, are its points of inflection?