

1. **(6 points)** You are hoping to save up \$100,000 by judicious, periodic investments into an interest-bearing account over the next 20 years. You intend to make two contributions per year into an account that bears 2.4% annual interest compounding semiannually. How large does your periodic semiannual contribution need to be in order to achieve your goal?

Here you are building up an investment, so you want to use a formula for periodic contributions towards future accumulation, not a formula for periodic payments on a loan. The desired formula will thus be $A = \frac{Fi}{(1+i)^m - 1}$, and in this case $F = \$100,000$, $r = 0.024$, and $t = 20$. Since interest and contribution are both semiannual, $n = 2$ and thus $i = \frac{0.024}{2} = 0.012$ and $m = 20 \times 2 = 40$, leading to the calculation $A = \frac{\$100,000 \times 0.012}{1.012^{40} - 1} = \boxed{\$1962.50}$. If you wish to sanity-check your result, consider that 40 contributions of \$1962.50 is a total contribution of \$78,500, which is less than your goal of \$100,000 but within a plausible distance for the interest payments to be making up the shortfall.

2. **(5 points)** You have borrowed \$3000 at an annual interest rate of 4.5% compounding annually, to be repaid with four equal payments of \$836.23 over the next four years. Complete the following amortization schedule, rounding each quantity to the nearest cent.

Year	Starting balance	Payment	Interest	Principal repaid	Ending balance
1	\$3,000.00	\$836.23	\$135.00	\$701.23	\$2,298.77
2	\$2,298.77	\$836.23	\$103.44	\$732.79	\$1,565.98
3	\$1,565.98	\$836.23	\$70.47	\$765.76	\$800.22
4	\$800.22	\$836.23	\$36.01	\$800.22	\$0.00

3. **(4 points)** A house costs \$165,000 and you are putting 15% down to buy it and taking out a 30-year mortgage at an annual rate of 2.875% with 1.5 points on the loan. Determine, labeling which is which, the size of your down payment and the initial size of the loan.

The down payment of 15% is $\$165,000 \times 0.15 = \boxed{\$24,750}$. The remainder to be borrowed is $\$165,000 - \$24,750 = \$140,250$. To get 1.5 points on this loan, we want a loan of which 1.5% is points and of which the remaining 88.5% is the house-buying loan; that is to say, we want some loan value, 98.5% of which is \$140,250. Thus our total loan will be $\frac{\$140,250}{0.985} = \boxed{\$142,385.79}$.

4. **(5 points)** You have a \$600 debt on a credit card with a 24% annual interest rate compounding monthly. If you make a payment of \$30 towards your credit card debt each month (and make no more purchases with the card), how many months will it take you to pay off the debt?

The monthly interest rate is $i = \frac{24\%}{12} = 0.02$, the loan principal $P = \$600$, and the monthly payment is $A = 30$, so the number of months to discharge the debt is

$$m = \frac{-\log\left(1 - \frac{Pi}{A}\right)}{\log(1+i)} = \frac{-\log\left(1 - \frac{600 \times 0.02}{30}\right)}{\log(1.02)} \approx 25.79$$

which rounds up to $\boxed{26}$ months.