

1. Prove that there are no integers a and b such that $21a + 30b = 1$ (note that integers can be negative).
2. Prove by contradiction that if b is an integer such that $b \nmid k$ for every natural number k , then $b = 0$.
3. Prove by contradiction that $\log_5 8$ is irrational.